



Evol 1,2 - Adiabática

$$Q_{12} = 0 \quad \Delta S_{12} = 0$$

Evol 2-3 - P cte

$$Q_{23} = \Delta H_{23} = \frac{\gamma}{\gamma-1} nR(T_3 - T_2) > 0 ; \quad \Delta S_{23} = \frac{\gamma nR}{\gamma-1} \ln \frac{T_3}{T_2}$$

Evol. 3,4 - T cte

$$Q_{34} = T_3 nR \ln \frac{V_4}{V_3} > 0 \quad \Delta S_{34} = nR \ln \frac{V_4}{V_3}$$

Evol 4,1 $\frac{H}{P} = \text{cte}$, $\frac{T}{P} = \text{cte} = \nu$

$$Q_{41} = \Delta \tilde{E}_{i41} = \frac{nR}{\gamma-1} (T_1 - T_4) < 0 \quad \Delta S_{41} = \frac{nR}{\gamma-1} \ln \frac{T_1}{T_4}$$

Aquí que $\eta = 1 - \frac{|Q_{41}|}{Q_{23} + Q_{34}} = 1 - \frac{\frac{nR}{\gamma-1} (T_4 - T_1)}{\frac{\gamma}{\gamma-1} nR(T_3 - T_2) + T_3 nR \ln \frac{V_4}{V_3}}$

$$\rightarrow \sum \Delta S = 0 \rightarrow \frac{\gamma nR}{\gamma-1} \ln \frac{T_3}{T_2} + nR \ln \frac{V_4}{V_3} + \frac{nR}{\gamma-1} \ln \frac{T_1}{T_4} = 0 \quad (1)$$

$$\frac{\tilde{E}_{i3}}{\tilde{E}_{i2}} = \frac{\frac{nR}{\gamma-1} T_3}{\frac{nR}{\gamma-1} T_2} = \frac{T_3}{T_2} = \beta \quad (2)$$

En la evol. 1,2 : $\frac{T_1}{T_2} = \left(\frac{V_2}{V_1}\right)^{\gamma-1} = \alpha^{\gamma-1}$

$$\frac{T_1}{T_4} = \frac{T_1}{T_3} = \frac{T_1}{T_2} \frac{T_2}{T_3} = \frac{\alpha^{\gamma-1}}{\beta} \quad (3)$$

De (1) $\ln \frac{V_4}{V_3} = -\frac{1}{\gamma-1} \left[\ln \left(\frac{T_3}{T_2}\right)^{\gamma} + \ln \frac{T_1}{T_4} \right]$ " $\frac{V_4}{V_3} = \frac{1}{\left(\frac{T_3}{T_2}\right)^{\gamma/\gamma-1} \left(\frac{T_1}{T_4}\right)^{1/\gamma-1}}$

De (2) y (3): $\frac{V_4}{V_3} = \frac{1}{\beta^{\gamma/\gamma-1} \frac{\alpha^{\gamma-1}}{\beta}^{\gamma/\gamma-1}} = \frac{1}{\alpha \beta}$

Sustituyendo en la expresión del rendimiento

$$\eta = 1 - \frac{1 - T_1/T_4}{\gamma \left(1 - \frac{T_2}{T_3}\right) + (\gamma-1) \ln \frac{V_4}{V_3}} = 1 - \frac{1 - \frac{\alpha^{\gamma-1}}{\beta}}{\gamma \left(1 - \frac{1}{\beta}\right) - (\gamma-1) \ln(\alpha \beta)}$$